



The estimation of PID controller parameters of vector controlled induction motor using Ziegler-Nichols method

E. Başer^{1,a}, Y. Altun¹

¹Duzce University, Computer Engineering, Duzce, Turkey.

Accepted 25 May 2015

Abstract

Induction motors (IM) are commonly used in industrial applications due to their superiorities such as low cost, less maintenance requirements, high efficiency and high power density in comparison with other electric motors such as dc motors. There are many studies in the literature on IM control. The best known speed control method of the IM is scalar control method (SCM) because of its easy to understand and implement. The another control method which is known as vector control method is the field oriented control method (FOC). Although FOC is more sophisticated than SCM, it is higher performance on control in general. In this study, the mathematical model of IM has used on simulation and FOC method has implemented on it. Then for speed control of IM Ziegler-Nichols method is used. Matlab/Simulink software has used to simulate system.

Keywords: Induction motor; vectrol control; ziegler-nichols method; Simulink

1. Introduction

The use of induction motors is widespread in industry due to their simple structure and simple maintenance compared to other electric drives such as dc motors. With the development on the power electronic technology and control theories by using many control algorithms such as vector control and direct torque control the performance of IM has become more superior [1]. There are many control methods on IM such as SCM and FOC. FOC method has superiorities than SCM due to high performance on control [2]. PID

controllers can used to control speed of IM. Although PID controllers have simple structure, many control loops used today are PID controllers [3]. There are a lot of studies about designing PID parameters [4-10]. The most useful method to determine PID controller parameters is Ziegler - Nichols method [4]. In literature there are many studies to improve PID controller parameters which has designed by using Ziegler-Nichols method. In this study it has tried to control speed of three phase induction motor on Matlab/Simulink software. Speed results has shown on figures.

^a Corresponding author;

Phone: +90-543-231-1149, Email: ekrembaser@duzce.edu.tr

2. Material and Methods

Firstly, to implement FOC to induction motor mathematical model of induction motor has investigated from its equivalent circuit. The equivalent circuit of IM has shown on Figure-1. Equialevent circuit shown on dq axis. From this equialevent circuit this equations has generated.

$$v_{sd} = R_s i_{sd} - w_d \lambda_{sq} + L_{ls} \frac{d}{dt} i_{sd} + L_m \frac{d}{dt} (i_{sd} + i_{rd}) \quad (1.1)$$

$$v_{sq} = R_s i_{sq} - w_d \lambda_{sd} + L_{ls} \frac{d}{dt} i_{sq} + L_m \frac{d}{dt} (i_{sq} + i_{rq}) \quad (1.2)$$

$$v_{rd} = R_r i_{rd} - w_{dA} \lambda_{rq} + L_{lr} \frac{d}{dt} i_{rd} + L_m \frac{d}{dt} (i_{sd} + i_{rd}) \quad (1.3)$$

$$v_{rq} = R_r i_{rq} - w_{dA} \lambda_{rd} + L_{lr} \frac{d}{dt} i_{rq} + L_m \frac{d}{dt} (i_{sq} + i_{rq}) \quad (1.4)$$

EElectromagnetic torque;

$$T_{em} = -\frac{p}{2} \lambda_{rd} i_{rq} = \frac{p}{2} \lambda_{rd} \left(\frac{L_m}{L_r} i_{sq} \right) \quad (1.5)$$

p is the pole number
Rotor d axis winding;

$$\frac{d}{dt} \lambda_{rd} + \frac{\lambda_{rd}}{\tau_r} = \frac{L_m}{\tau_r} i_{sd} \quad (1.6)$$

τ_r is called rotor time constant.

Stator Fluxes is written in a vector form

$$\frac{d}{dt} \begin{bmatrix} \lambda_{sd} \\ \lambda_{sq} \end{bmatrix} = \begin{bmatrix} v_{sd} \\ v_{sq} \end{bmatrix} - R_s \begin{bmatrix} i_{sd} \\ i_{sq} \end{bmatrix} - \omega_d \underbrace{\begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}}_{Mrotate} \begin{bmatrix} \lambda_{sd} \\ \lambda_{sq} \end{bmatrix} \quad (1.7)$$

Mechanical rotor of speed;

$$\frac{d}{dt} W_{mech} = \frac{T_{em} - T_L}{J_{eq}} \quad (1.8)$$

Synchronous speed;

$$w_{syn}(t) = w_m(t) + w_{slip}(t) \quad (1.9)$$

θ Angel;

$$\theta_{B_r}(t) = 0 + \int_0^t w_{syn}(\tau) \cdot d\tau \quad (1.10)$$

abc-dq transform;

$$\begin{bmatrix} d \\ q \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} \cos\theta & \cos\theta - 2\frac{\pi}{3} & \cos\theta - 4\frac{\pi}{3} \\ \sin\theta & \sin\theta - 2\frac{\pi}{3} & \sin\theta - 4\frac{\pi}{3} \end{bmatrix} \quad (1.11)$$

dq- abc transform;

$$\begin{bmatrix} a \\ b \\ c \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} \cos\theta & -\sin\theta \\ \cos\theta + 4\frac{\pi}{3} & -\sin\theta \\ \cos\theta + 2\frac{\pi}{3} & -\sin\theta + 2\frac{\pi}{3} \end{bmatrix} + 4\frac{\pi}{3} \begin{bmatrix} d \\ q \end{bmatrix} \quad (1.12)$$

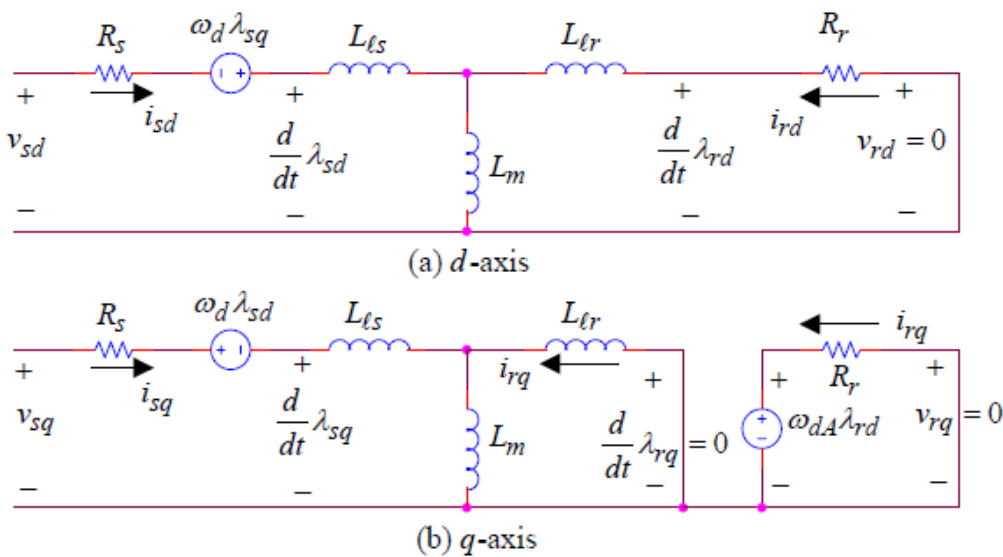


Figure 1. Equivalent circuit of IM on dq axes.

Simulink model of IM has generated from this Figure-2. equations[11] on Matlab/Simulink software as shown

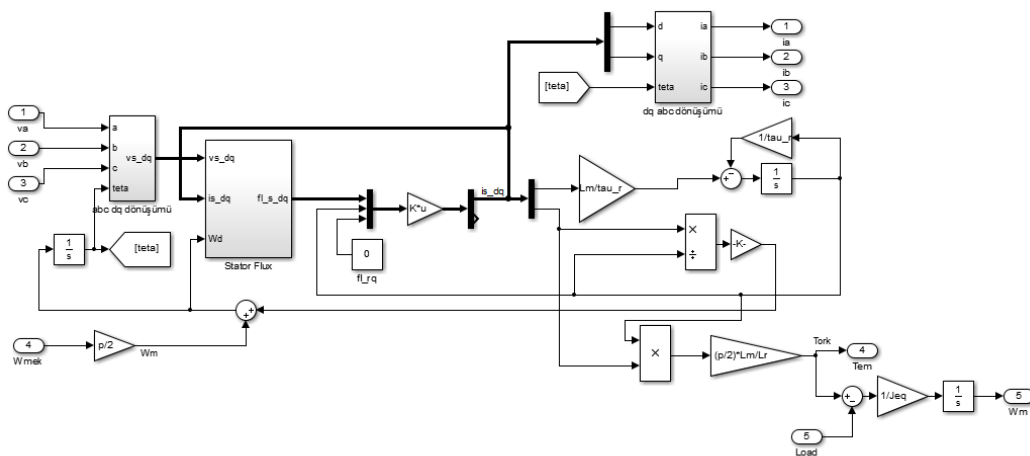


Figure 1. IM model block.

The parameters and nameplates of IM which has simulated here are listed below.

- Power : 3 HP/2.4 kW
- Voltage : 460 V
- Frequency : 60 Hz
- Phase: : 3
- Tüm Yüklemedeki Çektiği Akım:4A
- Tam Yüklemedeki Hızı : 1750 Rpm
- Verimliliği : %88.5
- R_s : 1.77Ω
- R_r : 1.34Ω
- X_{ls} : 5.25Ω
- X_{lr} : 4.57Ω
- X_m : 139Ω

J_{eq} : 0.025kg.m²

According to field oriented control theory, a reference mechanical speed has given initially to system. Then by PI controlling with which measured from motor. current has obtained. has given 0 initially. and voltages has calculated by controlling reference currents. For controlling three phase induction motor this and voltages has transformed from dq axis to abc axis. voltage has given to induction motor and motor has driven with this three phase voltages. In Figure-3 a classic vector control block scheme has shown. Simulink implementation of this control method also has shown Figure-4.

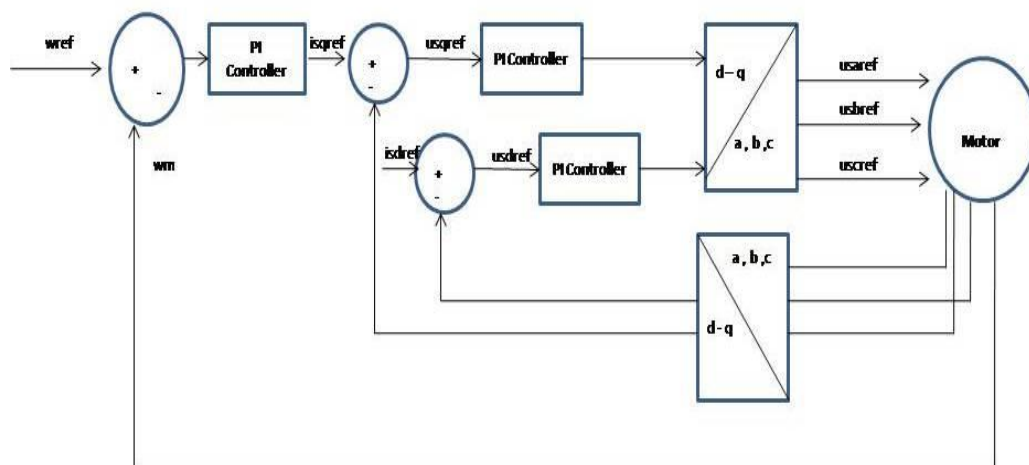


Figure 2 Vector control block scheme.

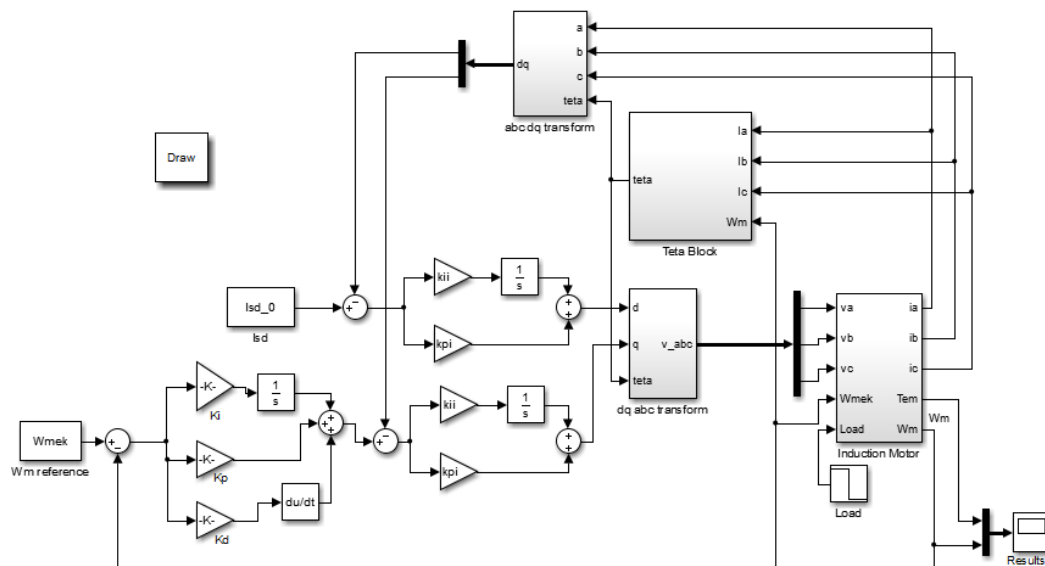


Figure 3 Vector controlled IM simulation.

Ziegler-Nichols method is a technique that tries to find parameters by trial and error. System is driven by using only P controller initially and slowly increased

until persistent oscillation is reached. At this point value is marked as and the period between two oscillation is denoted as . In Figure-5 IMs mechanical

speed which is reached oscillation by slowly increasing value has shown. At this point and values has

founded like below.

$$\tilde{T} = 0,025 - 0,017 = 0,08$$

$$\tilde{K}_p = 26$$

Then, PID controller parameters has calculated according to Ziegler-Nichols parameter calculation method as shown Table-1.

$$K_p = 0.6\tilde{K}_p = 0.6 * 26 = 15.6$$

$$K_i = \frac{\tilde{T}}{2} = \frac{0.008}{2} = 0.004$$

$$K_d = \frac{\tilde{T}}{8} = \frac{0.008}{8} = 0.001$$

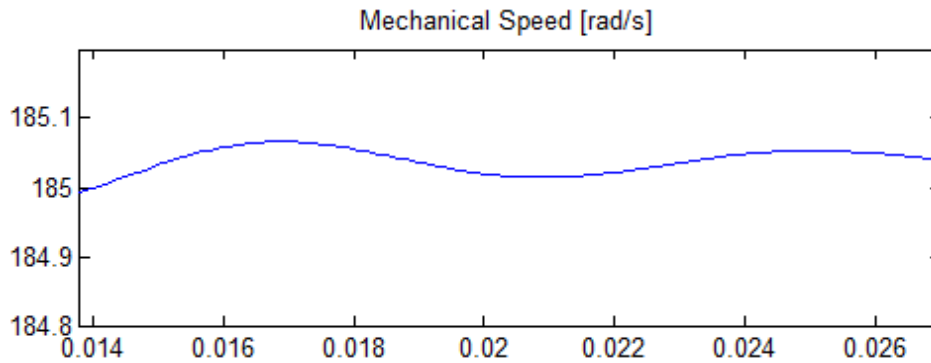


Figure 4 Oscillation state.

Table 1. Ziegler-Nichols method PID parameters calculation

Controller Type	K_p	K_i	K_d
P Controller	$0.5\tilde{K}_p$	∞	0
PI Controller	$0.45\tilde{K}_p$	$\tilde{T}/1.2$	0
PID Controller	$0.6\tilde{K}_p$	$\tilde{T}/2$	$\tilde{T}/8$

3. Results

Calculated K_p , K_i , K_d parameters has used speed control loop of this vector control block of simulation model and the speed graphic of IM has obtained as

Figure-6. At the 0.1 time point the load torque has affected to IM and has tried to change IM mechanical speed. In this figures it is shown that speed of IM has controlled by using Ziegler-Nichols method.

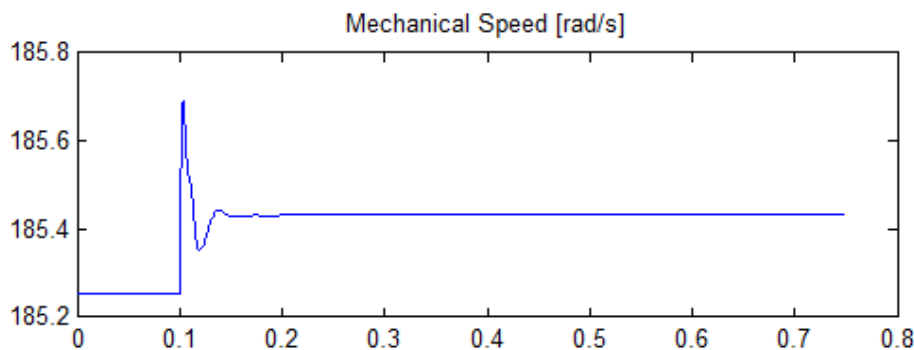


Figure 5 Mechanical speed graph.

4. Conclusion

In this study, speed control of the induction motor has been tried to simulate by using Ziegler-Nichols method on Matlab/Simulink software. Ziegler Nichols

method has been successful on designing parameters and controlling IM speed.

Acknowledgement

This study was supported by Duzce University Scientific Research Projects Coordinatorship. Project No: 2015.06.01.295.

References

- [1] Wang, X., Yang, Y., & Liu, W. (2011, June). "Simulation of vector controlled adjustable speed System of induction motor based on Simulink. In Computer Science and Service System (CSSS), 2011 International Conference on (pp. 2563-2566). IEEE.
- [2] Krein, P. T., Disilvestro, F., Kanellakopoulos, I., & Locker, J. (1993, June). Comparative analysis of scalar and vector control methods for induction motors. In Power Electronics Specialists Conference, 1993. PESC'93 Record., 24th Annual IEEE (pp. 1139-1145). IEEE.
- [3] Åström, K. J., & Hägglund, T. (2001). The future of PID control. *Control engineering practice*, 9(11), 1163-1175
- [4] Bhattacharyya, S. P., Datta, A., & Ho, M. T. (2000). Structure and synthesis of PID controllers.
- [5] Ackermann, J., & Kaesbauer, D. (2001, September). Design of robust PID controllers. In European control conference (pp. 522-527).
- [6] Shafiei, Z., & Shenton, A. T. (1997). Frequency-domain design of PID controllers for stable and unstable systems with time delay. *Automatica*, 33(12), 2223-2232.
- [7] Zadeh, L. A. (1965). Fuzzy sets. *Information and control*, 8(3), 338-353.
- [8] Zadeh, L. (1984). Making computers think like people: the term fuzzy thinking is pejorative when applied to humans, but fuzzy logic is an asset to machines in applications from expert systems to process control. *Spectrum*, IEEE, 21(8), 26-32.
- [9] Lee, C. C. (1990). Fuzzy logic in control systems: fuzzy logic controller. II. *Systems, Man and Cybernetics*, IEEE Transactions on, 20(2), 419-435.
- [10] O'Dwyer, A. (2000). A summary of PI and PID controller tuning rules for processes with time delay. Part 2: PID controller tuning rules.
- [11] Mohan, N. (2001). *Advanced electric drives—analysis, modeling and control using Simulink*. Minneapolis, MN: Minnesota Power Electronics Research & Education.